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## **Newton-Raphson Method: Approach and Applications**

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### Abstract

**Purpose:** The Newton-Raphson method (NRM) is a significant problem in statistics, Computational Mathematics, Applied Mathematics, and many other scientific fields, such as Engineering, Economics, and Decision Sciences, because its applications are extremely rich and diverse. This method can help scholars and practitioners solve some specific problems.

**Design/methodology/approach:** This method is widely used in Science because of its outstanding features. To contribute to the literature on this issue, this study details specific applications of the NRM.

**Findings:** We presented the most detailed Newton-Raphson method (NRM). We discuss its applications in practical problems, Statistics, Applied Mathematics, and other Sciences.

**Originality/value:** This study provides detailed and meaningful applications of the NRM for the first time.

**Practical implications:** This study aims to detail specific applications of the NRM. Four scenarios of applying the NRM to practical problems, Statistics, Applied Mathematics, and other Sciences are discussed in detail.

Keywords: Newton-Raphson method, Application, real problems, Mathematics.

JEL classifications: A10, G00, G31, O32

**Article type: Research article** 

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