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Research Article

An Experimental Research Study on the Solution of a Private Small Hydropower Plant Investments Selection Problem by ELECTRE III/IV, Shannon's Entropy, and Saaty's Subjective Criteria Weighting

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Almost all of the today's modern daily life conditions of humankind depend on the electricity. The countries either by only themselves or sometimes with some international intuitions and/or organizations have been trying to find the best methods, ways, and projects to supply the electricity to their societies. One of the important tools for the countries to increase the amount and quality of the electricity generation is to activate/ignite/initiate the private investment capabilities/opportunities. The electricity generation market in Turkey is a free/open market for both the foreign and domestic private investors. Hence, both the foreign and domestic private investors have been looking for the most suitable electricity generation plant projects. Small hydropower plant (SHPP) investments (SHPPIs) are one of the alternatives in the Turkish electricity generation market especially for the private investors searching for the renewable energy investments. This experimental research study investigates the possibility of using the ELECTRE III/IV, Shannon's Entropy, and Saaty's Analytic Hierarchy Process (AHP) subjective weighting (for criteria) methods for the solution of this problem. In the experimental case study, the most appropriate SHPPIs amongst five alternative SHPPIs at the SHPPIs' predevelopment investment stages in Turkey were evaluated and ranked in order.

1. Introduction

The peak load and the electricity consumption in Turkey have been increasing in almost steady conditions since 1996 as presented in Table 1. The causes of this almost steady electricity demand increase condition are mainly given as the increase in the population in Turkey and the increase in the income growth in Turkey by the researchers (see and read some studies on this issue [1–3]).

These increasing conditions of the population and the gross domestic product (GDP) in Turkey are presented by the help of the historical data as shown in Figure 1 for expressing and showing the actual situation of these conditions very clearly and plainly to the researchers, the academics, the private investors, and the whole readers.

In addition to these historical data, several projection studies for these two indicators present that the growth status will continue in the long term (see and read some studies on this issue [1–3]).

The location of Turkey is very interesting and strategic in the point of view of the geographical, geopolitical, and socioe-conomic research studies (see and read [4–6]). Turkey is a transcontinental (Europe and Asia) country that has the land boundaries with Syria (822 km) (southeast), Iran (499 km) (east), Iraq (352 km) (southeast), Armenia (268 km) (east), Georgia (252 km) (northeast), Bulgaria (240 km) (northwest), Greece (206 km) (west), and Azerbaijan (9 km) (east) (see and read [7]). Turkey can be grouped under several geographical and socioeconomic regions such as the Balkans (Bulgaria, Greece, etc.) (see and read [8]), the Caucasus

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TABLE 1: The peak load and the electricit	y consumption of Turkish Interconnected Electricity System.
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Year	Peak load (MW)	Percent change (%)	Electricity consumption (GWh)	Percent change (%)
1996	15.231	7.5	94.789	10.8
1997	16.926	11.1	105.517	11.3
1998	17.799	5.2	114.023	8.1
1999	18.938	6.4	118.485	3.9
2000	19.390	2.4	128.276	8.3
2001	19.612	1.1	126.871	-1.1
2002	21.006	7.1	132.553	4.5
2003	21.729	3.4	141.151	6.5
2004	23.485	8.1	150.018	6.3
2005	25.174	7.2	160.806	7.2
2006	27.594	9.6	174.637	8.6
2007	29.249	6.0	190.000	8.8
2008	30.517	4.3	198.085	4.3
2009	29.870	-2.1	194.079	-2.0
2010	33.392	11.8	210.434	8.4
2011	36.122	8.2	229.319	9.0

Data and source [14, 15].

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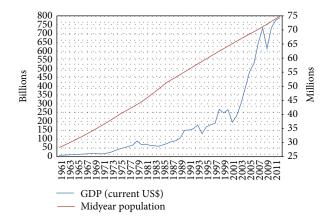


FIGURE 1: GDP: gross domestic product and population in Turkey (generated by the Microsoft Office Excel 2007). *Data*: GDP (current USD, 1961–2012) [12] (left axis), midyear population estimations (1961–2012) [13] (right axis).

Region (Azerbaijan, Georgia, etc.) (see and read [9]), the Europe (France, Germany, etc.) (see and read [10]), and the MENA Region (Middle East and North Africa: Egypt, Morocco, etc.) (see and read [11]). This geographical location also gives an advantage to Turkey to interconnect its national electricity grid to the other national electricity grids, which also increases very much the importance of the current subject of this experimental research study, not only for the perspective of Turkey, but also for the perspective of the regions, such as the Balkans, the Caucasus, and the MENA.

The Turkish electricity generation establishments can be grouped according to their management styles, organization structures, sizes, and business capabilities. The diversified characteristics and properties of these entities in the Turkish electricity generation market make the business and management models and organizations classification study not

so difficult. The decision making process of these entities are different from each other based on these characteristic differences. The application and adaptation of several appropriate scientific methods are very important for some entities, so that the more the research studies by the different approaches and methods are conducted in this subject, the more the appropriate scientific methods and approaches will be started to be used and preferred in the decision making process of the private small hydropower plant investments (PSHPPIs) in the practical daily life, which will expectedly increase the total satisfaction on the PSHPPIs of all of the participants, the parties, and the involvers.

The entities or the investors in the Turkish electricity generation sector can either invest in the renewable energy sources (RESs) main group or in the fossil fuels sources main group. The hydropower and the wind power in the RESs main group and the natural gas and the imported coal in the fossil fuels main group have the major pie or share groups in this market. The projected installed capacity by the primary energy resources is presented in Figure 2.

The hydropower plants are grouped as one segment without considering their installed capacities (each power plant) in this projection. Figure 2 shows that the total percentage or share of the installed capacity of the hydropower plants in Turkey shall be increased or tried to be increased to almost 40% of the total installed power of the whole power plants in Turkey until 2020s, which indicates and means that the subject of this experimental research study will keep its importance in the short to long terms and periods. Generally, the hydropower plants are classified based on their installed capacities (P) as large, medium, small, mini-, micro-, and picohydropower plants. However, the consensus on the installed capacities of this classification has not been achieved yet. For instance, the SHPP installed capacity (kW) was presented as (P < 10.000) by Dragu et al. [33], (P < 10.000)by EREC [34], $(1.000 < P \le 10.000)$ by ESHA [35],

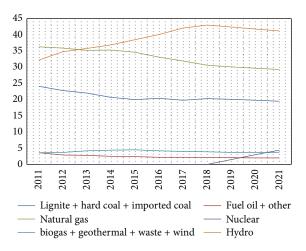


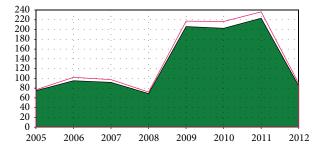
FIGURE 2: Projected installed capacity (average of scenarios 1 and 2) in Turkey (% of MW) (generated by the Microsoft Office Excel 2007). *Data*: [14, 15].

 $(2.000 < P \le 25.000)$ by Mishra et al. [36], and $(3.000 < P \le 25.000)$ by Ramachandra and Shruthi [37].

In the current study, the SHPPs were accepted as the hydropower plants that had the installed capacity of $1.000 \,\mathrm{kW} < P \leq 10.000 \,\mathrm{kW}$. The EMRA's (Republic of Turkey Energy Market Regulatory Authority) official website (http://www.emra.gov.tr/ or http://www.epdk.gov.tr/) had been visited several times before this experimental research study was started. There were 212 SHPPs with the total installed electrical power of 1.048 MWe until September 2012 under the investigation and evaluation stage of the license application procedure (see Figure 3 for the SHPPs' applications to EMRA cumulative by year). The foreign, domestic, and local private investors (foreign: investors from all over the world such as Austria, Norway, and England; domestic: investors from Turkey; local: investors from Artvin) were able to investigate, select, invest, and have in their SHPPI portfolio (some of the megawatts) from the PSHPPI alternatives as shown in Figure 3.

The presented data and the socioeconomic conditions prove and show the reasons, why the investors have searched for the private SHPP investments (PSHPPIs) as the long term real sector investment alternatives. Small to large size private investors (establishments or real people) with different strategic investment plans have tried to find the PSHPPIs for having some or whole of the shares. Some of the investors have also looked for several numbers of PSHPPIs to have them as one group.

In this respect, the main objective and the main problem of the private investors that should be solved in the most appropriate, convenient, simple, and understandable ways (please keep in mind that there may be several ways, not only one way) for the private investors are to find and select the most satisfying PSHPPIs on the point of view of the private investors' (in a more scientifically clear clause or statement: the decision makers of the private investors or the private investors by themselves) understanding, perception, and character amongst the possible alternative PSHPPIs. For



- Installed power (electrical power) (MWe)
- □ Installed power (mechanical power) (MWm)

FIGURE 3: SHPPs' applications to EMRA (Latest 2012 September) (generated by the Microsoft Office Excel 2007). *Data*: [14] (only official website).

instance, the intentions of the different private investors (a private investor may be an institutional investor, a legal entity, a national or international joint venture, and a single natural person or a group of them) are very different from each other (for instance, the net profit maximization in the short term or the risk minimization in the long term) that makes them to take into account and consideration very different factors during the solution of the finding and selection problem of the PSHPPIs. The main aim of this study is to contribute to the scientific studies by defining the PSHPPIs' selection problem and presenting an experimental research for its solutions.

In this paper, a private SHPPs' investment selection problem in Turkey was solved by mainly help of the ELECTRE (Elimination and Choice Translating Reality: Elimination Et Choix Tradusiant la Realite) methods (one of the Multicriteria Decision Making (MCDM) methods). The objective and subjective weighting methods were adopted for the decision of the criteria weights or the voting power of the factors only. In the current experimental research case study, there were five private SHPP alternative investments (PSHPPIs), which the titles were not presented, because of the possibility of the continuity of their commercially sensitive situations, in Turkey. However, the sufficient data and information were presented for the readers to make them understand the experimental research case very well.

This paper consists of four sections. The methods are presented by the literature review in the next section. The experimental research case study is explained and the experimental research case study results are given in the third section. Finally, the conclusions and future research are discussed and presented in Section 4.

2. Materials and Methods

The previous studies in the literature were reviewed in the explicated twofold framework as presented in Figure 4.

The previous studies in the first fold framework were reviewed on some scientific online database websites (all fields' option selected) by help of the selected keywords until the 1st of January in 2014. The literature review in the first

WSP

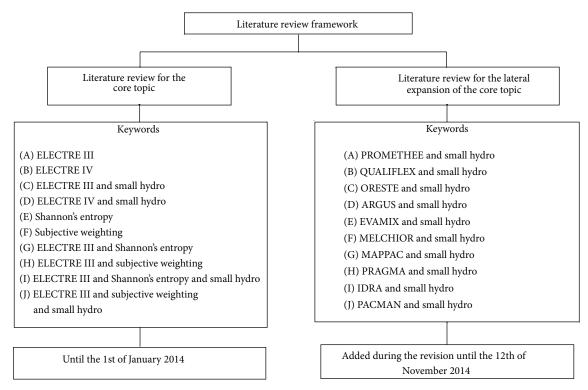


FIGURE 4: The literature review framework of the current experimental research study (generated by the Apache OpenOffice 4.1.0 Draw).

Key terms Scientific publisher (A) (B) (C) (D) (E) (F) (G) (H) (I) (J) **ACMDL** n **ASCEOR ASME** CJO DOAJ n ΕI 8* 1.156 SD TFJ 1* WB

TABLE 2: Summary of the literature review in the first fold framework.

Data and source: ACM Digital Library (ACMDL) (http://dl.acm.org/), ASCE Online Research Library (ASCEOR) (http://ascelibrary.org/), ASME (http://asmedigitalcollection.asme.org/), Cambridge Journals Online (CJO) (http://journals.cambridge.org/), DOAJ (http://doaj.org/), Emerald Insight (EI) (http://www.emeraldinsight.com/), Science Direct (SD) (http://www.sciencedirect.com/), Taylor & Francis Journal (TFJ) (http://www.tandfonline.com/), Wiley-Blackwell (WB) (http://onlinelibrary.wiley.com/), and World Scientific Publishing (WSP) (http://www.worldscientific.com/).

Keywords: (A): ELECTRE III, (B): ELECTRE IV, (C): ELECTRE III and small hydro* (aim and scope difference with the current study), (D): ELECTRE IV

and small hydro, (E): Shannon's entropy, (F): subjective weighting, (G): ELECTRE III and Shannon's entropy, (H): ELECTRE III and subjective weighting, (I): ELECTRE III and Shannon's entropy and small hydro, and (J): ELECTRE III and subjective weighting and small hydro.

fold framework showed that this paper would most probably be one of the first studies in its aim and scope (see Table 2).

The previous studies in the second fold framework were reviewed on the same scientific online database websites with the same search options by help of the new selected keywords until the 12th of November in 2014. The keywords or key phrases included the set of the other outranking methods such as the PROMETHEE (Preference Ranking

Organization METHod for Enrichment Evaluations), the QUALIFLEX (QUALItative FLEXible), the ORESTE (Organization, Rangement Et Synthese De Donnes Relationnelles), the ARGUS (Achieving Respect for Grades by Using ordinal Scales), the EVAMIX (Evaluation of Mixed Criteria), the MELCHIOR (Méthode d'ELimination et de Choix Incluant les relation d'ORdre), the MAPPAC (Multicriterion Analysis of Preferences by Means of Pairwise Actions and Criterion

Scientific publisher	Ablisher Key terms									
Scientific publisher	(A)	(B)	(C)	(D)	(E)	(F)	(G)	(H)	(I)	(J)
ACMDL	0	0	0	0	0	0	0	0	0	0
ASCEOR	0	0	0	0	0	0	0	0	0	0
ASME	0	0	0	0	0	0	0	0	0	0
CJO	0	0	0	0	0	0	0	0	0	0
DOAJ	0	0	0	0	0	0	0	0	0	0
EI	0	0	0	0	0	0	0	0	0	0
SD	21*	0	2*	15*	0	3*	0	2*	0	0
TFJ	1*	0	0	1*	0	1*	0	0	0	0
WB	1*	0	1*	0	0	0	0	0	0	0
WSP	0	0	0	0	0	0	0	0	0	0

TABLE 3: Summary of the literature review in the second fold framework.

Data and source: ACM Digital Library (ACMDL) (http://dl.acm.org/), ASCE Online Research Library (ASCEOR) (http://ascelibrary.org/), ASME (http://asmedigitalcollection.asme.org/), Cambridge Journals Online (CJO) (http://journals.cambridge.org/), DOAJ (http://doaj.org/), Emerald Insight (EI) (http://www.emeraldinsight.com/), Science Direct (SD) (http://www.sciencedirect.com/), Taylor & Francis Journal (TFJ) (http://www.tandfonline.com/), Wiley-Blackwell (WB) (http://onlinelibrary.wiley.com/), and World Scientific Publishing (WSP) (http://www.worldscientific.com/).

Keywords: (A): PROMETHEE and small hydro* (aim and scope difference with the current study), (B): QUALIFLEX and small hydro, (C): ORESTE and small hydro* (aim and scope difference with the current study), (D): ARGUS and small hydro* (aim and scope difference with the current study), (E): EVAMIX and small hydro, (F): MELCHIOR and small hydro* (aim and scope difference with the current study), (G): MAPPAC and small hydro, (H): PRAGMA and small hydro* (aim and scope difference with the current study), (I): IDRA and small hydro, and (J): PACMAN and small hydro.

Comparisons), the PRAGMA (Preference RAnking Global frequencies in Multicriteria Analysis), the IDRA (Intercriteria Decision Rule Approach), and the PACMAN (Passive and Active Compensability Multicriteria Analysis) (see the outranking methods in [38]). The literature review in the second fold framework presented that this paper would most probably be one of the first studies in the usage and application of the outranking methods for solving the problem explained in this study (see Table 3), which ought to have encourage to work on these presented outranking methods in Table 3 in the future research studies.

The first ELECTRE (ELimination Et Choix Traduisant la REalité: ELimination and Choice Expressing the REality) method (ELECTRE I: electre one), which was founded on the outranking approach (the European school approach), was proposed in the 1960s by Bernard Roy (the inventor of the family of ELECTRE methods) (1934-alive by November 2014), who was the founder of the LAMSADE and the researchers at the European consultancy company SEMA (Société d'Économie et de Mathématiques Appliquées) (British and French information technology merger) (see also LAMSADE (Laboratoire d'Analyse et Modélisation de Systèmes pour l'Aide à la DEcision: http://www.lamsade.dauphine.fr/) in France [39]. Afterwards, new versions of this method were evolved [39, 40]. The ELECTRE Iv (electre one vee) added a veto threshold into the method, and the ELECTRE IS (electre one esse) dealt with the imperfect data [40]. The ELECTRE II (electre two) was developed for solving the problems of ranking actions [40, 41]. The ELECTRE III (electre three) was introduced as a more developed one using the pseudocriteria (the thresholds q_i and p_i , the imprecision, and the uncertainty) instead of the true-criteria (the smallest difference in performances makes a strict preference between the comparisons of the alternatives) and the fuzzy binary

outranking relations for ranking actions [40, 42, 43]. The ELECTRE IV (electre four) was developed to deal with the problems without working on the relative criteria importance coefficients (unwillingness to present information on the role of the criteria) [40, 41, 44]. The ELECTRE TRI (electre tree), the ELECTRE TRI-B, the ELECTRE TRI-C, the ELECTRE TRI-NC, and the ELECTRE GMS were the latest ELECTRE methods [41, 44]. The ELECTRE III [38, 40–45] and the ELECTRE IV [38, 40, 41, 44] methods are based on the following principles.

The alternatives or actions or options with only partially known a priori are $A = \{a_1, a_2, \dots, a_i, \dots, a_m\}$, where m is potential finite number of alternatives or actions.

The family of defined pseudocriteria is $F = \{g_1, g_2, ..., g_i, ..., g_n\}$ where $n \ge 3$.

The performance of actions or alternatives a_i on the pseudocriterion g_i is $g_i(a_i)$ for all $a_i \in A$ and $g_i \in F$.

The binary outranking relations are I (indifference: reflexive and symmetric relation), P (strict preference: nonreflexive and asymmetric relation), Q (weak preference (hesitation): nonreflexive and asymmetric relation), and R (incomparability: nonreflexive and symmetric relation). The partial binary outranking relations are shown in Figure 5.

 q_j is the indifference threshold, p_j is the preference threshold, and v_j is the veto threshold with respect to the jth criterion ($v_j \ge p_j \ge q_j$: for maximization criteria and for minimization additive inverse).

The researchers and the readers should be aware of the difficulties of choosing the realistic threshold values in the ELECTRE methods [46].

 q_j is the highest value that beyond this value the difference is clear for the human perception [46].

 p_j may be selected as at least twice as q_j for a case that is the symmetrical about the mean value [46].

$$\mathbf{a_k} \mathbf{I_j} \mathbf{a_n} \text{: } (\mathbf{a_k} \text{ is indifferent to } \mathbf{a_n}) \qquad \Leftrightarrow \qquad |g_j(\mathbf{a_k}) - g_j(\mathbf{a_n})| \leq q_j \qquad \forall (\mathbf{a_k}, \mathbf{a_n}) \in \mathbf{A}$$

$$\mathbf{a_k} \mathbf{P_j} \ \mathbf{a_n} \text{: } (\mathbf{a_k} \text{ is strictly preferred to } \mathbf{a_n}) \qquad \Leftrightarrow \qquad g_{\mathbf{j}} \left(\mathbf{a_k} \right) > g_{\mathbf{j}} \left(\mathbf{a_n} \right) + p_{\mathbf{j}} \qquad \forall (\mathbf{a_k}, \mathbf{a_n}) \in \mathbf{A}$$

$$(\mathbf{a_k})$$
 $(\mathbf{a_n})$ $(\mathbf{a_k})$ is weakly preferred to $\mathbf{a_n})$ \Leftrightarrow $q_{\mathbf{i}} < g_{\mathbf{i}}(\mathbf{a_k}) - g_{\mathbf{i}}(\mathbf{a_n}) \le p_{\mathbf{i}} \quad \forall (\mathbf{a_k}, \mathbf{a_n}) \in \mathbf{A}$

$$(a_k)$$
 (a_n)

 $\mathbf{a_k} \mathbf{R_j} \, \mathbf{a_n} \!\!: (\mathbf{a_k} \text{ is incomparable to } \mathbf{a_n}) \qquad \qquad \text{Otherwise} \qquad \qquad \forall (\mathbf{a_k}, \mathbf{a_n}) \in \mathbf{A}$

Figure 5

 v_j may be selected as at least three times as p_j [46]:

The voting power of
$$g_j$$
 is w_j and $\sum_{\{j|g_j\in F\}} w_j = 1$. (1)

The group of the strict preference relation, the weak preference relation, and the indifference relation is the partial binary outranking relation: $S_i = P_i \cup Q_i \cup I_i$ ($\succ_i = Q_i \cup P_i$).

The comprehensive outranking relation is $S = P \cup Q \cup I$ (>= $Q \cup P$):

$$\mathbf{a_k} \mathbf{S} \mathbf{a_n}$$
 and not $(\mathbf{a_n} \mathbf{S} \mathbf{a_k})$:

$$(a_k \succ a_n) \Longleftrightarrow (a_k \text{ is preferred to } a_n)$$

$$\forall (\mathbf{a_k}, \mathbf{a_n}) \in A,$$

 $a_n S a_k$ and not $(a_k S a_n)$:

$$(a_n > a_k) \iff (a_n \text{ is preferred to } a_k)$$

$$\forall (\mathbf{a_k}, \mathbf{a_n}) \in A, \tag{2}$$

 $a_k S a_n$ and $a_n S a_k$:

$$\mathbf{a_k} \mathbf{I} \mathbf{a_n} \Longleftrightarrow (\mathbf{a_k} \text{ is indifferent to } \mathbf{a_n})$$

$$\forall (\mathbf{a_k}, \mathbf{a_n}) \in A$$

not (a_kSa_n) and not (a_nSa_k) :

 $a_k R a_n \iff (a_k \text{ is incomparable to } a_n)$

$$\forall (\mathbf{a_k}, \mathbf{a_n}) \in A.$$

The concordance index (the strength of the positive arguments) of the actions or the alternatives (a_k, a_n) (the values of concordance matrix) is

$$c_{j}(a_{k}, a_{n})$$

$$= \begin{cases} 0, & \text{if } g_{j}(a_{k}) \leq g_{j}(a_{n}) - p_{j}, \\ 0 < \frac{p_{j} - \left[g_{j}(a_{n}) - g_{j}(a_{k})\right]}{p_{j} - q_{j}} < 1, \\ & \text{if } g_{j}(a_{n}) - p_{j} < g_{j}(a_{k}) < g_{j}(a_{n}) - q_{j}, \\ 1, & \text{if } g_{j}(a_{k}) \geq g_{j}(a_{n}) - q_{j}. \end{cases}$$

$$(3)$$

The total or overall or global or comprehensive concordance index is

$$C(a_k, a_n) = \frac{\sum_{j=1}^{n} w_j \times c_j(a_k, a_n)}{\sum_{j=1}^{n} w_j},$$
 (4)

where w_i is the weight of the criterion.

The discordance index (the strength of the opposition) of alternatives (a_k, a_n) is

$$d_{j}(a_{k}, a_{n}) = \begin{cases} 0, & \text{if } g_{j}(a_{k}) \geq g_{j}(a_{n}) - p_{j}, \\ 0 < \frac{p_{j} - \left[g_{j}(a_{n}) - g_{j}(a_{k})\right]}{p_{j} - v_{j}} < 1, \\ & \text{if } g_{j}(a_{n}) - v_{j} < g_{j}(a_{k}) < g_{j}(a_{n}) - p_{j}, \\ 1, & \text{if } g_{j}(a_{k}) \leq g_{j}(a_{n}) - v_{j}. \end{cases}$$

$$(5)$$

The creditability or the credibility or the credit degree $\sigma_s(a_k, a_n)$ is

$$\overline{F}\left(a_{k},a_{n}\right)=\left\{j\in F\mid d_{j}\left(a_{k},a_{n}\right)\geq C\left(a_{k},a_{n}\right)\right\},$$

$$\sigma_{s}\left(a_{k},a_{n}\right)$$

$$=\begin{cases}C\left(a_{k},a_{n}\right),\\C\left(a_{k},a_{n}\right)\prod_{j\in \overline{F}}\frac{1-d_{j}\left(a_{k},a_{n}\right)}{1-C\left(a_{k},a_{n}\right)}, & \text{if } \overline{F}\left(a_{k},a_{n}\right)\neq\emptyset.\end{cases}$$

$$\sigma_{s}\left(a_{k},a_{n}\right)=\begin{cases}1, & \text{if } a_{k}S_{q}a_{n},\\0.8, & \text{if } a_{k}S_{q}a_{n},\\0.6, & \text{if } a_{k}S_{p}a_{n},\\0.35, & \text{if } a_{k}S_{p}a_{n},\\0.35, & \text{if } a_{k}S_{q}a_{n},\\0.35, & \text{i$$

The network relation in the ELECTRE III/IV methods is based on $\sigma_s(a_k, a_n) \ge \lambda$.

The λ is called as the cut level and calculated by the highest credibility index and the discrimination threshold. If $\sigma_{\rm s}(a_k,a_n)$ is above the λ cut level (0.50 $\leq \lambda \leq$ 1.00, often $\lambda = 0.67$) then a_k outranks a_n . The λ -strength and the λ weakness is calculated for the ranking procedure. The ranking is based on the descending distillation (from the best to the worst) and the ascending distillation (from the worst to the best). The qualification is gathered by these calculations. The final ranking can be found by the average of distillation chains [47].

There are four levels of binary outranking relations in the ELECTRE IV method as the quasidominance relation (S_a) , the canonical-dominance relation (S_c) , the pseudodominance relation (S_p) , and the veto-dominance relation (S_v) (in some improved ones the subdominance relation (S_s) is added as the fifth relation) [48, 49]. The ELECTRE IV is not the form of ELECTRE III with the equal criteria weights. The algorithm of the ELECTRE IV method is as follows [49, 50]:

> $m_p(a_k, a_n)$: the number of criteria for which a_k is strictly preferred to a_n ;

> $m_a(a_k, a_n)$: the number of criteria for which a_k is weakly preferred to a_n ;

> $m_i(a_k, a_n)$: the number of criteria for which a_k is indifferent to a_n ;

> $m_o(a_k, a_n) = m_o(a_n, a_k)$: the number of criteria for which a_k has the same evaluation to a_n .

For any pair of alternatives (a_k, a_n) ,

$$m = m_{p}(a_{k}, a_{n}) + m_{q}(a_{k}, a_{n}) + m_{i}(a_{k}, a_{n}) + m_{o}(a_{k}, a_{n}) + m_{p}(a_{n}, a_{k}) + m_{q}(a_{n}, a_{k}) + m_{i}(a_{n}, a_{k}),$$
(7)

where *m* is the total number of criteria. Consider

$$\begin{split} S_q &: \text{if } m_p(a_n, a_k) + m_q(a_k, a_n) = 0 \text{ and } m_i(a_n, a_k) \leq 1 + \\ m_i(a_k, a_n) + m_q(a_k, a_n) + m_p(a_k, a_n) \text{ then } a_k S_q a_n; \end{split}$$

$$S_c$$
: if $m_p(a_n, a_k) = 0$ and $m_q(a_n, a_k) \le m_p(a_k, a_n)$ and $m_q(a_n, a_k) + m_i(a_n, a_k) \le 1 + m_i(a_k, a_n) + m_q(a_k, a_n) + m_p(a_k, a_n)$ then $a_k S_c a_n$;

$$S_p$$
: if $m_p(a_n, a_k) = 0$ and $m_q(a_n, a_k) \le m_q(a_k, a_n) + m_p(a_k, a_n)$ then $a_k S_p a_n$;

$$S_v$$
: if $m_p(a_n, a_k) = 0$ and $a_k S_p a_n$ or $m_q(a_n, a_k) = 1$ and no $a_n P V_j a_k \ \forall j$ and $m_p(a_k, a_n) \ge (m/2)$ in which $a_n P V_j a_k$: $(g_j(a_n) < g_j(a_k) + v_j(g_j(a_k))$ then $a_k S_v a_n$.

The creditability or the credibility or the credit degree

$$\sigma_{s}(a_{k}, a_{n}) = \begin{cases} 1, & \text{if } a_{k}S_{q}a_{n}, \\ 0.8, & \text{if } a_{k}S_{c}a_{n}, \\ 0.6, & \text{if } a_{k}S_{p}a_{n}, \\ 0.35, & \text{if } a_{k}S_{v}a_{n}, \\ 0, & \text{if no relation amongs } S_{q}, S_{c}, S_{p}, S_{v}. \end{cases}$$
(8)

There are several objective weight assessment methods such as the extreme weight approach, the random weight approach, and the entropy methods [51]. One of the most appropriate applicable methods is presented as the entropy methods amongst the objective weight assessment methods [51]. There are some criticisms about the entropy methods' closeness to the true weight vector according to the multiplicative error and the additive error when the decision makers' decisions are based on the exponential scale [52]. Despite these criticisms, Shannon's Entropy [53] (Shannon Information by Claude Elwood Shannon so called "the father of information theory") (1916-2001) as below amongst several developed entropy methods such as De Luca and Termini, Szmidt and Kacprzyk [54] was used for the criterion weight assessments in this experimental research study. Shannon's Entropy method was specifically preferred to be used, adopted, and investigated in the current experimental research study to understand the nature and performance of this objective weight assessment method for solving the defined problem in this experimental research study and to observe and predict its adoptability and its usage possibility in the future more sophisticated models (on the research, development, and deployment edge: the computer based intelligent decision making system and the autonomous decision making systems) for the real world cases. The method is shortly as follows [54-57].

The initialized decision matrix is $X = (x_{ij})_{n \times m}$, where *i* is for the criteria $(1 \le i \le n)$ and j is for the alternative $(1 \le j \le n)$

The normalized matrix is $R = (r_{ij})_{n \times m}$.

The elements of the normalized matrix r_{ij} take the values between 0 and 1 where

$$r_{ij} = \frac{x_{ij} - \min_{i} \left\{ x_{ij} \right\}}{\max_{i} \left\{ x_{ij} \right\} - \min_{i} \left\{ x_{ij} \right\}}$$

(for the criterion which is a kind of maximization),

$$r_{ij} = \frac{\max_{i} \left\{ x_{ij} \right\} - x_{ij}}{\max_{i} \left\{ x_{ij} \right\} - \min_{i} \left\{ x_{ij} \right\}}$$

(for the criterion which is a kind of minimization).

The entropy is e_i (note in general H, H(p(x), or H(A))) of the ith criterion as

$$e_{i} = -k \sum_{j=1}^{m} f_{ij} \ln \left(f_{ij} \right),$$
where $f_{ij} = \frac{r_{ij}}{\sum_{j=1}^{m} r_{ij}}, \quad k = \frac{1}{\ln (m)},$
when $f_{ij} = 0 \Longrightarrow f_{ij} \ln \left(f_{ij} \right) = 0,$

the weight of entropy of *i*th criterion as $w_i = \frac{1 - e_i}{n - \sum_{i=1}^n e_i}$,

where
$$0 \le w_i \le 1$$
, $\sum_{i=1}^{n} w_i = 1$. (10)

The subjective criteria weighting by Saaty's AHP (Analytic Hierarchy Process by Thomas L. Saaty) (1926-alive by November 2014) that was based on the pairwise comparisons of the criteria, the geometric mean approximation, and the normalization [58–60] was also used for the criterion weight assessments in this experimental research study. Saaty's AHP method (as for the subjective weight assessment method) was especially chosen to be employed and applied in this experimental research study, because of its capability of taking the experts' thoughts in a free and scientific way according to the experts' experiences and preferences.

Despite the ELECTRE methods have the main recommendation of being applied up to thirteen criteria, it is believed that the current experimental research case study (seventeen criteria) can also be handled with ease by the ELECTRE methods.

The ELECTRE III (for ranking decision), the ELECTRE IV (for ranking decision), Shannon's Entropy (for voting power decision), and Saaty's AHP subjective criteria weighting (for voting power decision) methods were applied and tested in the experimental research case study as presented in the next section.

3. The Experimental Research Model, Case, Results, and Discussion

The ELECTRE methods are very effective for solving the problems with large number of actions or alternatives [38–46]. However, only five candidate private SHPP investments in the predevelopment investment stages were investigated during this experimental research case study. The data and information of these candidate PSHPPIs were collected and evaluated according to ten subjective and seven objective criteria. The experimental research model was built and performed by both Microsoft Excel (http://www.microsoft.com) and Apache OpenOffice Calc software (http://www.openoffice.org/). The model files of the experimental research case study in *.xls and *.ods formats were also available for the readers (correspond and contact to the author and also see the electronic supplementary material). Moreover, it should be mentioned that the electrical

installed capacity *P* (in Watts: W) (see and read [61]) of a SHPP was calculated by the following formula:

$$P = \eta_{\rm tr} \times \eta_g \times \eta_t \times \rho_w \times g \times Q \times H, \tag{11}$$

where η_{tr} is efficiency of transformer, η_g is efficiency of generator, η_t is efficiency of turbine, ρ_w is density of water (kg/m³), g is gravity (m/s²), Q is design/project discharge (m³/s), and H is net head (m) (J: Joule, kg: kilogram, m: meter, N: Newton, s: second, W: Watt) (W = J/s = N * m/s = kg * m²/s³) (for extraction of this formula/equation see and read [18, 62, 63]).

The criteria in the current experimental research study were selected as given in Table 4 based on the state of mind in the positive thinking (please look for the state of mind and the positive thinking terms see and read [64–68]).

The major concentration, interest, effort, and working hours (spent hours) in this experimental research study was not mainly spent on finding, defining, identifying, describing, and selecting the PSHPPIs' selection factors or criteria; instead the main focus and the core research interest of the current experimental research study were applying and testing the mentioned and noticed methods, observing and deeply understanding their ability, capability, and usability, and analyzing their performance on reflecting the decision makers preferences and opinions on the selection of the PSHPPIs' problem area, learning their difficulties for the future real world applications (very large number of criteria sets and actions sets) and solving this experimental case problem. Henceforth, the criteria or factors on this experimental research model were found, gathered, and selected from the previous research studies of the author (please correspond to and contact to the author from the presented e-mail address to get more information about those previous research studies (published/under review/under revisions review/yet unpublished stages) on those subjects). The objective criteria (Cr: criterion) in this experimental research study were such as the catchment area (Cr01), which was taken into account in the current experimental model, because it was one of the important elements that could be affected by the climatic conditions and at the same time influenced the project runoff and the flow rate; the project runoff (Cr02) that was considered in the current experimental model, because it showed the water flown over the earth's surface, generated mainly by the rainfall and the snow, and affected the flow rate; the net head (Cr03) that was examined in the current experimental model, because it was one of the items that defined the types of the electromechanical equipment and their operation conditions, and at the same time it was a direct variable of the installed capacity and the electricity generation by the PSHPPs; the flow rate (Cr04), which was studied in the current experimental model, because it presented the amount of water that could be run through the water turbines at the defined specific duration, and at the same time it was a direct variable of the installed capacity and the electricity generation by the PSHPPs; the firm energy (Cr05) and the secondary energy (Cr06) that were taken into account in the current experimental model, because they determined directly the gross income or the earnings (so that the net income) of the

Table 4: The criteria description.

	Cr*	Criterion	SOM**	MM^{+}	S [#]	Description
	Cr01	Catchment area (km²)	nc	ma	n	The approximate numerical value was taken from information form (General Directorate of State Hydraulic Works: http://www.dsi.gov.tr) of the SHPP (for the term [16]).
	Cr02	Project runoff (hm³)	nc	ma	n	The approximate numerical value was taken from information form (for this term [17]).
	Cr03	Net head (m)	nc	ma	n	The approximate numerical value was taken from information form (for this term [16]).
Objective	Cr04	Flow rate (m ³ /s)	nc	ma	n	The approximate numerical value was taken from information form (for this term visit [16])
criteria	Cr05	Firm energy (GWh)	nc	ma	n	The power delivered during a certain period of the day with at least 90–95% certainty" [18]. The approximate numerical value was taken from information form.
	Cr06	Secondary energy (GWh)	nc	ma	n	The approximate numerical value was taken from information form.
	Cr07	Investment cost (million USD)	nc	mi	n	The approximate numerical value was taken from information form. The total estimated investment cost was in US Dollars. The exchange rate was taken from the Central Bank of the Republic of Turkey (http://www.tcmb.gov.tr) on 8th of September in 2013.
	Cr08	River basin	ptd	ma	ls	The main river basins of the projects were evaluated by the EDMs based on their knowledge and experience.
	Cr09	Conveyance structure	ptd	ma	ls	The conveyance structures of the SHPP projects were evaluated according to the knowledge and the experiences of the EDMs (for this term [19]).
	Cr10	Community attitude	ptd	ma	ls	The local community supportive or opposition opinion about the SHPPs was investigated in this criterion.
	Cr11	Transportation	ptd	ma	ls	The availability, flexibility, quality, and conditions of all the transportation modes were evaluated by the EDMs based on their knowledge and experience.
Subjective	Cr12	Topography	ptd	ma	ls	The surface shapes and features of SHPPs' site were evaluated by the EDMs.
criteria	Cr13	Geology	ptd	ma	ls	The geological conditions and properties of SHPPs' site were evaluated by the EDMs.
	Cr14	Security conditions	ptd	ma	ls	The public security, the infrastructure security, and other security groups were evaluated based on the theft, the burglary, and other security risks and threats (see [20, 21]) by the EDMs.
	Cr15	Terrorism conditions	ptd	ma	ls	The perceived terrorism risks and threats (see [22, 23]) were evaluated by the EDMs.
	Cr16	Protected areas	ptd	ma	ls	The natural parks, the ecological values, and so forth were evaluated by the EDMs.
	Cr17	Substation conditions	ptd	ma	ls	The conditions of the grid connection were evaluated by the EDMs.

^{*}Cr: code, **SOM: state of mind, nc: no condition because of objective criteria, ptd: positive thinking direction, [†]MM: maximization/minimization: maximization, mi: minimization, [‡]S: scale: n: numerical scale, ls: 5-point Likert scale: 1 to 5: the worst to the best, and EDM: expert decision maker. See and visit [24] for square kilometer (km²), [25] for cubic hectometer (hm³), [26] for meter (m), [27] for cubic metre per second (m³/s), [28] for gigawatt hour (GWh), [29] for million, and [30] for USD.

PSHPPs; and finally the investment cost (Cr07), which was evaluated in this experimental model, so that the financial or economic performance of the PSHPPIs would be tried to be estimated by considering both the income (as a whole) and the cost (as a whole) at the same time. All of these criteria were evaluated concurrently in the current experimental model for not missing and omitting any important issues, subjects, topics, and points and at the same time for having

the consistent data and information set, so that it aims to be placed in the safe analysis and investigation actions or alternatives space for the electricity generation amount of the PSHPPIs. The subjective criteria in this experimental research study were such as the river basin (Cr08) (for example, Meric-Ergene River Basin, Marmara River Basin, and Susurluk River Basin in Turkey), which was studied in the current experimental model to put the characteristics and the future

Action	Cr01 (km²)	Cr02 (hm³)	Cr03 (m)	Cr04 (m³/s)	Cr05 (GWh)	Cr06 (GWh)	Cr07 (Million USD)	Cr09
A1	79	47	369	3	26	15	11,5	Channel closed rectangular 3.900 m
A2	61	48	388	3	6	31	7,8	uPVC pipe 3.300 m
A3	329	131	172	8	16	38	16,6	Channel open rectangular 9.600 m
A4	130	133	135	10	14	29	24,1	Tunnel modified horseshoe 8.800 m
A5	553	701	97	19,5	29	23	27,9	Tunnel circular 5.900 m

TABLE 5: The PSHPPIs actions in this experimental case study.

See and read [24] for square kilometer (km²), [25] for cubic hectometer (hm³), [26] for meter (m), [27] for cubic metre per second (m³/s), [28] for gigawatt hour (GWh), [29] for million, and [30] for USD; see, read, and watch [31] and see and read [32] for some issues about the conveyance structures.

conditions and predictions of the river basins into this model; the conveyance structure (Cr09) (for example, a long tunnel, a short tunnel, an open channel, and several tunnels) that was preferred to be evaluated to try to foresee the difficulties and the obstacles mainly during the construction period and the operation period; the community attitude (Cr10), which was considered in the current experimental model for predicting the supporting activities, the oppositions, the blockages, and the protests against the PSHPPI; the transportation (Crl1) that was evaluated in this experimental model for the difficulties before the construction period, during the construction period and during the operational period; the topography (Cr12), which was put into the current experimental model for the difficulties and the easiness of the activities for the construction and the investigations and the engineering studies before the construction period, during the construction and operational periods; the geology (Cr13), which was taken into account in the current experimental model, because the activities and all of the design and construction works were related with this factor; the security conditions (Cr14) that was considered in this experimental model for predicting the difficulties such as the security risks and threats for the private life, the public life, and the infrastructure before the construction period and during the construction and operational periods; the terrorism conditions (Cr15) that were taken into account because of the same reasons with the security conditions, but with a devastating effect such as the civil disorder, the political, the nonpolitical, the ideological, and the official or state terrorisms; the protected areas (Cr16) (for example, the cultural values, the natural parks, the important bird areas, and the rainforests) that was evaluated for predicting the permission works and also the community attitude and at the same time for having environmentally friendly, compatible, and responsible PSHPPs; and finally the substation conditions (Cr17), which was studied for analyzing the connection to the grid possibilities and conditions before and during the construction period and the easiness and the ability of the operation and the maintenance of the connection lines during the construction period. All of these criteria were thought to be evaluated by the healthy, honest, fair, reliable, straightforward, trustworthy, and pragmatic experts

and decision makers (in other words not ill, unhealthy, dishonest, unfair, unreliable, unreasonable, insincere, and untrustworthy) under the normal conditions (for instance, not under any duress, coercion, threat, violence, mobbing, and bullying).

The actions or alternatives or options in the current experimental research study were found and taken from the PSHPPIs portfolio in Turkey (please consider, think, and imagine all of the private power plants in Turkey as a whole private investment portfolio set for the real sectors' foreign or domestic or local private investors; moreover please keep in mind that the private small hydropower plants investment set is a subset of this whole private investment portfolio set), which could be accepted and assumed as free or available or ready to be sold or exchanged some of its shares and stocks in the predevelopment investment stages. The main characteristics of these actions were gathered from the PSHPPIs official records on the open sources as some of them presented in Table 5.

The experimental research model of the current study was founded on the EDM's preferences and evaluations; henceforth the main decision making process was supported by the ELECTRE III (ranking) and Saaty's AHP (voting power) (imagine like the highway); the experimental decision making process had three main sections or parts (imagine like the sideways) as the ELECTRE III (ranking) and Shannon's Entropy (voting power), the ELECTRE III (ranking) and the Equal Weighting (voting power), and the ELECTRE IV. In addition to these main sections (methods and approaches), three λ cut levels were used for the investigation and the analysis of the discrimination and the distinction of the actions or the alternatives in this experimental research study. The experimental research model was tried to be presented by the help of Figure 6.

In the current experimental case study, there were two experts, who were also the decision makers (a group decision making case). This condition made the use of the expert decision maker (EDM) term possible. The expert decision makers (EDM₁ and EDM₂: multidisciplinary experts) were capable of evaluating all of these criteria in a sufficient manner. The EDMs took their weighting power (weight of the

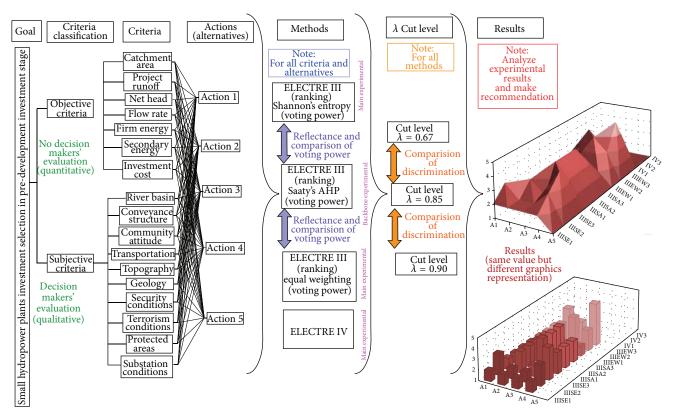


FIGURE 6: The experimental research model (generated by the Apache OpenOffice 4.1.0 Draw).

EDM) on the decision process by their practical experience in the industry and the educational background (bachelor, master, and doctoral degrees in the engineering fields).

The subjective criteria were evaluated by the Likert 5 type scale (by Likert: 1903–1981) [69] and the linguistic or verbal statements considering the basic principles of the human mind cognitive capacity such as the magical number 7, 7 ± 2 rule (by Miller (1920–2012), Shiffrin (1968-alive by November 2014) and Nosofsky (alive by November 2014)) [70, 71] and the verbal qualifiers (by Rohrmann (alive by November 2014)) [72] as presented in Table 6.

The criteria weights were found by Shannon's Entropy method (objective weighting) and by Saaty's AHP method (subjective weighting) as shown in Figure 7. The consistency ratios of the EDMs' evaluations were found as 9.9% and 9.7%, respectively, in Saaty's AHP method for the criteria weighting, which were less than 10% and in the acceptable levels. Shannon's Entropy method calculated the highest priority for the project runoff, the catchment area, the flow rate, and the community attitude criteria, respectively. The EDMs gave the highest priority to the terrorism, the substation, and the security, respectively, as calculated by Saaty's AHP method for the criteria. The difference of the values between Shannon's Entropy and Saaty's AHP method for the project runoff, the catchment area, the flow rate, the community attitude, the terrorism, the substation, and the security criteria were $0.1193 \text{ (EDM}_1)$ and $0.1155 \text{ (EDM}_2)$; 0.0780 (EDM₁) and 0.0782 (EDM₂); 0.0509 (EDM₁) and 0.0498 (EDM₂); 0.0639 (EDM₁) and 0.0658 (EDM₂); -0.1419 (EDM₁) and -0.1418 (EDM₂); -0.1111 (EDM₁) and -0.1235 (EDM₂); -0.1038 (EDM₁), -0.0864 (EDM₂), respectively. These experimental results showed that Shannon's Entropy method was not able to reflect exactly the EDMs' perception on the criteria calculated by Saaty's AHP method in this particular experimental case (Figure 7) (note: important finding for this experimental research model, and this experimental research case).

The EDM_1 took the weight of 0.4 and the EDM_2 took the weight of 0.6 by the agreed upon point of view and the consensus of the EDMs, because of being not only based on their experience and knowledge on the PSHPPIs, but also according to their specific and particular interest, attention, consideration, focus, and examination on the current experimental research case. The evaluations for all criteria of the EDMs were compared and checked with each other as presented in Figure 8.

The performance of the alternatives, the indifference thresholds, the preference thresholds, the veto thresholds and the criterion weights of criteria for the EDMs, and the percentage of the differences of these performances, thresholds, weights, and the characteristics of the EDMs made the aggregation process sufficiently acceptable and possible by (12) and (13) as the IDAMS (Internationally Developed Data Analysis and Management Software) of the UNESCO (United Nations Educational, Scientific and Cultural Organization) (see some issues for the principle approaches [73–82]).

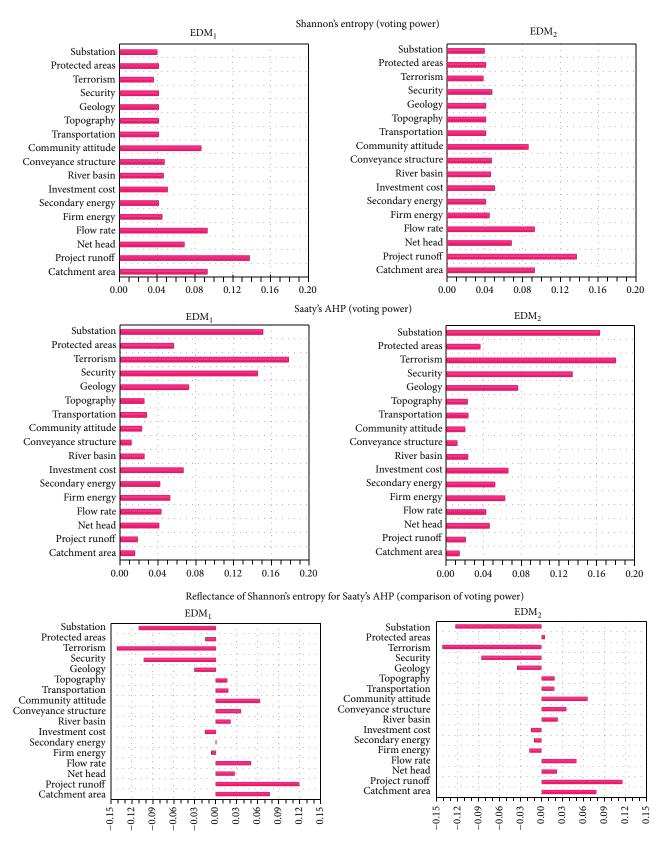


FIGURE 7: The objective and the subjective criteria evaluations by the EDMs (generated by the Microsoft Office Excel 2007).

	Subjective criteria		Action	s (alternatives	s)					
Code	Name	Direction of preference	A1	A2	A3	A4	A5			
	Expert decision maker 1 (EDM ₁)									
Cr08	River basin	Max	VB	G	В	VG	VG			
Cr09	Conveyance structure	Max	G	VG	A	VB	В			
Cr10	Community attitude	Max	A	В	G	VB	VB			
Cr11	Transportation	Max	VG	В	A	G	G			
Cr12	Topography	Max	VG	В	A	G	G			
Cr13	Geology	Max	G	В	VB	A	A			
Cr14	Security conditions	Max	VG	G	В	G	A			
Cr15	Terrorism conditions	Max	VG	A	VB	G	G			
Cr16	Protected areas	Max	В	A	VG	G	G			
Cr17	Substation conditions	Max	В	G	A	A	A			
		Expert decision make	r 2 (EDM ₂)							
Cr08	River basin	Max	VB	G	В	VG	VG			
Cr09	Conveyance structure	Max	G	VG	A	VB	В			
Cr10	Community attitude	Max	A	В	G	VB	VB			
Cr11	Transportation	Max	VG	В	A	G	G			
Cr12	Topography	Max	VG	В	A	G	G			
Cr13	Geology	Max	G	В	VB	A	A			
Cr14	Security conditions	Max	VG	G	В	A	A			
Cr15	Terrorism conditions	Max	VG	A	VB	A	G			
Cr16	Protected areas	Max	В	A	VG	G	G			
Cr17	Substation conditions	Max	В	G	A	A	A			

TABLE 6: The subjective criteria evaluation by the EDMs.

Linguistic or verbal statements.

(5) VG: very good; (4) G: good; (3) A: average; (2) B: bad; (1) VB: very bad.

The threshold values were defined based on the principles explained in the previous section as in Table 7. Consider

The concordance index:
$$c_j(a_k, a_n) = \frac{\sum_{z=1}^{yy} w_z \times c_{jz}(a_k, a_n)}{\sum_{z=1}^{yy} w_z}$$
, (12)

where z indicates the experts as $Z = \{z_1, z_2, \dots, z_i, \dots, z_{yy}\}$. Consider

The weight of the criterion:
$$w_j = \frac{\sum_{z=1}^{yy} w_z \times w_{jz}}{\sum_{z=1}^{yy} w_z}$$
,

The discordance index:
$$d_j(a_k, a_n) = \frac{\sum_{z=1}^{yy} w_z \times d_{jz}(a_k, a_n)}{\sum_{z=1}^{yy} w_z}$$
.

In the current experimental case study, the experimental model was built upon the consideration of the main features, the criticisms, the improvements, and the new approaches for the ELECTRE methods (see [44]). The credibility (degree) matrices of the ELECTRE III with the objective weighting (Shannon's Entropy), the ELECTRE III with the subjective weighting (Saaty's AHP), the ELECTRE III with the Equal Weighting, and the ELECTRE IV were calculated and presented as shown in Table 8.

The λ cut level was first selected as ($\lambda = 0.67$), then ($\lambda = 0.85$), and ($\lambda = 0.90$).

The decending distilation process and the ascending distilation process (upward and downward distilation) were calculated from the credibility matrices by the help of the sum of the elements of each row and the sum of the elements of each column. The sum of the elements in each row presented the strength of the criterion and the sum of the elements in each column showed the weakness of the criterion. The calculations were also checked by the help of the relation graphs as shown in Figures 9 and 10 (see the electronic supplementary material in the Supplementary Material available online at http://dx.doi.org/10.1155/2015/548460 for the whole details of the calculations).

The ranks for each method and for each λ cut level were gathered to make the final decision and to deeply understand and analyze the nature of the methods and the approaches in the current experimental research study as presented in Table 9.

The ELECTRE III (ranking) with Shannon's Entropy (voting power) in the 0.67 λ cut level gave the preference of the PSHPPIs (the rankings of the actions or the alternatives) as Action or Alternative 5 in the first rank, Action 1, Action 2, Action 3, and Action 4 in the second rank. The discrimination or separation or partition in this experimental case was not definite or distinct as only two preference or selection or rank sets (1 and 2) could be found in the results and findings. The rankings of the PSHPPIs in the 0.85 λ cut level were Action or Alternative 5 in the first rank, Action 2 and Action 3 in

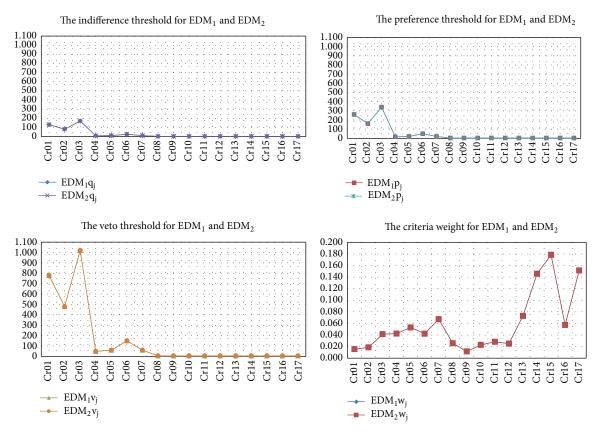


FIGURE 8: The indifference threshold, the preference threshold, the veto threshold, and the criteria weight of the EDMs (generated by the Microsoft Office Excel 2007).

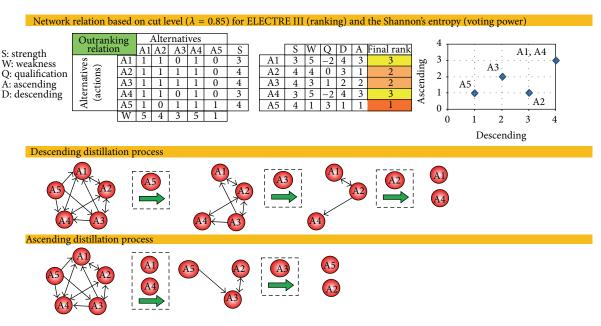


FIGURE 9: The descending distillation process and the ascending distillation process I (see the electronic supplementary material for the whole details of the calculations).

TABLE 7: The threshold values.

Criterion		EDM ₁		EDM_2				
Criterion	Indifference q_j	Preference p_j	Veto v_j	Indifference q_j	Preference p_j	Veto v_j		
Cr01	130	260	780	100	200	600		
Cr02	80	160	480	60	120	360		
Cr03	170	340	1.020	160	320	960		
Cr04	8	16	48	6	12	36		
Cr05	10	20	60	9	18	54		
Cr06	25	50	150	20	40	120		
Cr07	10	20	60	9	18	54		
Cr08-Cr17*	2	3	5	2	3	5		

^{*}Same value from Cr08 to Cr17.

TABLE 8: The creditability or the credibility degrees and matrix for all methods.

Methods			Credibil	ity matrices		
		A1	A2	A3	A4	A5
ELECTRE III	A1	1.000	0.953	0.829	0.904	0.000
(ranking)	A2	0.871	1.000	0.870	0.953	0.000
Shannon's Entropy	A3	0.858	0.978	1.000	0.938	0.000
(voting power)	A4	0.893	0.878	0.839	1.000	0.000
	A5	0.916	0.848	0.903	1.000	1.000
		A1	A2	A3	A4	A5
ELECTRE III	A1	1.000	0.976	0.931	0.966	0.000
(ranking)	A2	0.892	1.000	0.976	0.990	0.000
Saaty's AHP	A3	0.594	0.986	1.000	0.904	0.000
(voting power)	A4	0.929	0.915	0.967	1.000	0.000
	A5	0.920	0.887	0.965	1.000	1.000
		A1	A2	A3	A4	A5
ELECTRE III	A1	1.000	0.941	0.864	0.918	0.000
(ranking)	A2	0.823	1.000	0.923	0.978	0.000
Equal Weighting	A3	0.808	0.981	1.000	0.918	0.000
(voting power)	A4	0.879	0.866	0.894	1.000	0.000
	A5	0.917	0.837	0.929	1.000	1.000
		A1	A2	A3	A4	A5
	A1	1.000	0.000	0.000	0.000	0.000
ELECTRE IV	A2	0.000	1.000	0.000	0.000	0.000
LLL GITTE I	A3	0.000	0.000	1.000	0.800	0.000
	A4	0.000	0.000	0.800	1.000	0.000
	A5	0.000	0.000	0.000	0.000	1.000

the second rank, and Action 1 and Action 4 in the third rank. The discrimination in this one ($\lambda=0.85$) was more clear than the previous one ($\lambda=0.67$) as three selection sets (1, 2, and 3) could be found in the results and the findings. The rankings of the PSHPPIs in the 0.90 λ cut level were Action or Alternative 5 in the first rank, Action 1 and Action 3 in the second rank, Action 2 in the third rank, and Action 4 in the fourth rank. The discrimination in this one ($\lambda=0.90$) was the most recognizable and definite one ($\lambda=0.85$, $\lambda=0.67$) as four selection sets (1, 2, 3, and 4) could be found in the results and the findings. All of the final rankings in the

current experimental research study are presented in Figure 11 to give an a whole overview of the methods (for ranking and voting power) and the ranks. Action 5 was positioned in the first rank by all of the methods and λ cut levels according to the preferences (the indifference threshold, the preference threshold, the veto threshold, and the criteria weight) of the EDMs in this experimental research case (see Table 9). Action 1 was positioned in the second rank by all of the methods and λ cut levels except the ELECTRE III (ranking) with Shannon's Entropy (voting power) at the λ cut level of 0.85 and the ELECTRE IV based on the preferences of the EDMs (see

Methods	λ cut level	A1	A2	A3	A4	A5	Abbreviation on Figure 11
ELECTRE III	0.67	2	2	2	2	1	IIISE1
ELECTRE III Shannon's Entropy	0.85	3	2	2	3	1	IIISE2
onamions Entropy	0.90	2	3	2	4	1	IIISE3
ELECTEDE III	0.67	2	3	4	3	1	IIISA1
ELECTRE III Saaty's AHP	0.85	2	3	4	3	1	IIISA2
	0.90	2	3	4	3	1	IIISA3
ELECTEDE III	0.67	2	2	2	2	1	IIIEW1
ELECTRE III Equal Weighting	0.85	2	3	4	3	1	IIIEW2
Equal Weighting	0.90	2	4	3	5	1	IIIEW3
	0.67	1	1	1	1	1	IV1
ELECTRE IV	0.85	1	1	1	1	1	IV2
	0.90	1	1	1	1	1	IV3

Table 9: The ranks for each method and for each λ cut level.

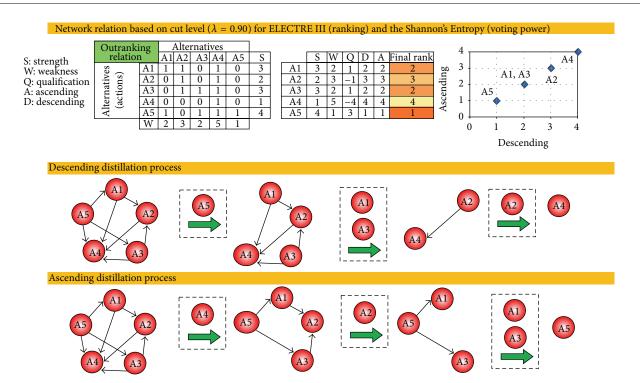
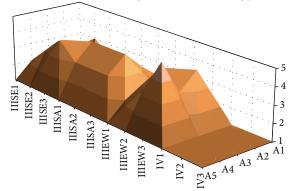


FIGURE 10: The descending distillation process and the ascending distillation process II (see the electronic supplementary material for the whole details of the calculations) (generated by the Microsoft Office Excel 2007).

Table 9). Action 2 was stood in the three highest, two lowest, and seven middle rank selection sets or classes. Action 3 had three highest ranks, three middle ranks, and six lowest ranks. Action 4 was included in three highest, four middle, and five lowest rank selection sets. It was observed in this experimental research study that the ELECTRE IV was not helpful for the discrimination or separation or partition of the current actions or alternatives under these preferences of the EDMs, so that the ELECTRE IV could not be expressed or accepted as a responsive or sensible or sensitive method in the current experimental research case. The ELECTRE III (ranking) with Saaty's AHP (voting power) method gave the same ranks and classification (Action 5: 1st, Action 1: 2nd;

Action 2 and 4: 3rd; Action 3: 4th) in all of the λ cut levels (λ = 0.67, λ = 0.85, and λ = 0.90). These findings and exploration on the ELECTRE III Saaty's AHP method showed that the λ cut levels did not make any difference in the results and the findings of this experimental research case. Moreover, this experimental research study presented that the reflectance of the ELECTRE III and Shannon's Entropy method and the ELECTRE III and the Equal Weighting method on the ELECTRE III and Saaty's AHP method got higher and higher values, while the λ cut levels got higher and higher values.

The final rankings and the overall results were also finally discussed by the EDMs in the current experimental research study and it was agreed upon that Action or Alternative 5 then



Surface view of the final ranks of the ranking methods and the voting power for each λ cut level

Bar chart view of the final ranks of the ranking methods and the voting power for each λ cut level

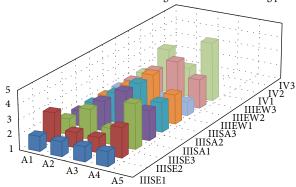


FIGURE 11: The final ranks of the experimental research case study (surface view: generated by the Microsoft Office Excel 2007, bar chart view: generated by the Apache OpenOffice Calc).

Action 1 took the highest ranks, Action 3 took the lowest rank, and Action 2 and Action 4 took the middle ranks. Henceforth, Action or Alternative 5 and the Action 1 had to be moved into the development investment stages of the PSHPPIs. The other alternatives had to be studied after these two PSHPPIs.

4. Conclusions, Future Applications, and Research

In this experimental research study, the solution of a private SHPP projects' investment selection problem in Turkey was tried to be solved by the help of mainly the ELECTRE III/IV methods. The EDMs tried to gather as much as support from the scientific methods, so that the criteria weights were defined by two different methods as the Shannon's Entropy and the Saaty's AHP. In addition to these calculations, the equal weight calculations for the ELECTRE III were performed to increase the number of the experimental methods for a better analysis and investigation for this experimental research study and the future research studies (on the research, development, and deployment edge: the computer based intelligent decision making system and the autonomous decision making systems). All of these studies empowered the EDMs to express their ideas and made their mind up in a correct manner. The EDMs realized that the decision on the value of the indifference threshold (q_i) , the

preference threshold (p_j) , and the veto threshold (v_j) was very difficult and crucial. Henceforth the special attention should be given to the evaluation of these thresholds in the future research studies.

This experimental research study should be followed by the evaluation of the thresholds study. All of the thresholds should be reevaluated, wherever necessary and the final decisions should be taken according to these renewed calculations. In addition, the current experimental case study should be performed based on only the subjective criteria and only the objective criteria. This study will show how the final decisions are generally affected by the subjective factors. Moreover, the number of criteria and the combinations of criteria should be reorganized and a new study should be done or performed. Afterwards, the studies should be performed for the different project stages such as the development stages in the small hydropower plant industry.

These kinds of research studies most probably will help the investors, the institutions, organizations (international and domestic), and the governments to invest in the most appropriate investments in the real sectors that will help to use the resources (financial, manpower, and mind power) as efficiently and effectively as possible. Hence, the appropriateness, the suitability, the convenience, and the coherence of these kinds of investment decisions in the real sectors can surely affect, impact, and touch on the most positive way to the upper most objectives of humankind such as

fighting against hunger and malnutrition, prevention of and fight against crime, keeping peace and security, respecting for justice and the rule of law, preserving human rights and freedom, improving health and wealth status.

Conflict of Interests

The author declares that there is no conflict of interests regarding the publication of this paper.

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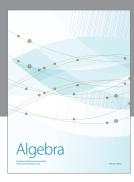
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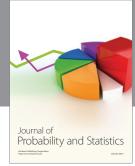
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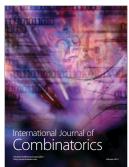






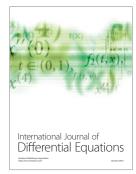




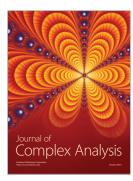




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